

# **Observing geocenter motion from LEO POD using onboard GPS tracking data**

**Da Kuang, Shailen Desai and Bruce Haines**

**Jet Propulsion Laboratory, California Institute of Technology**

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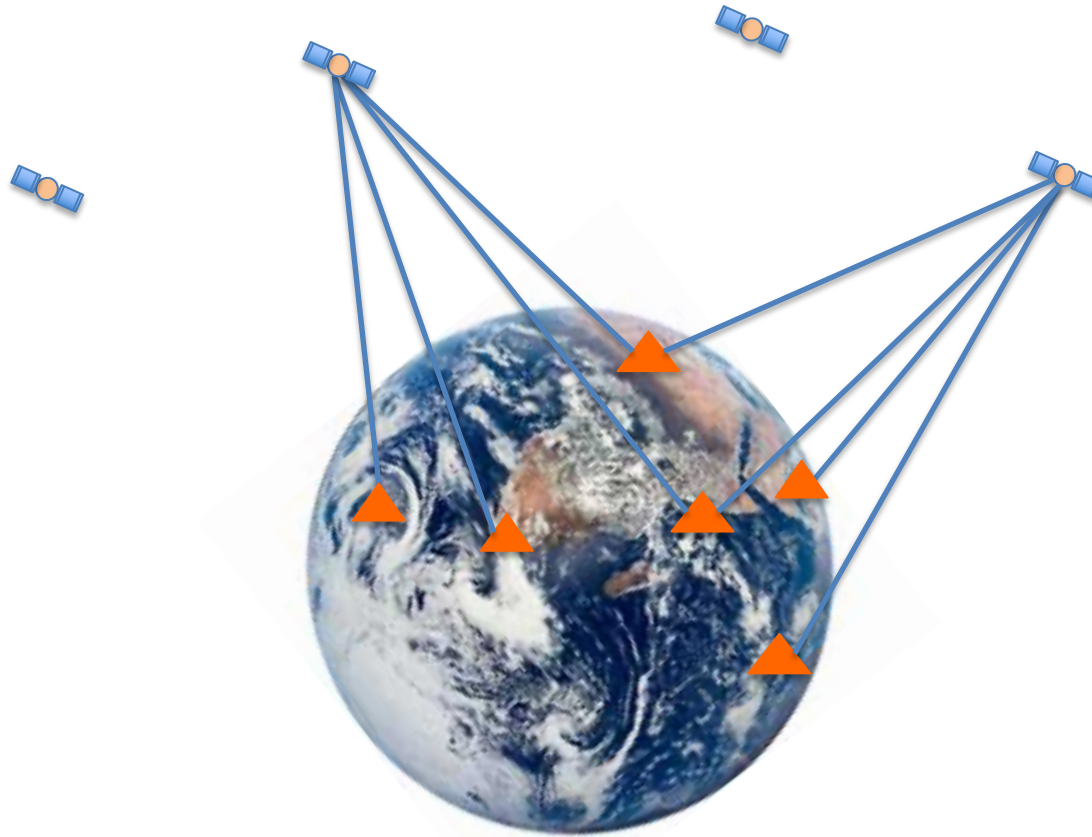
# Outline

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- **Reference frame in LEO orbit determination**
  - **IGS products disseminate reference frame to users**
  - **JPL “fiducial” product and geocenter motion**
  - **Estimating geocenter motion in LEO POD**
- **Observed geocenter motion**
  - **Result from GRACE POD with accelerometer data**
  - **Result from other satellites without accelerometer data**

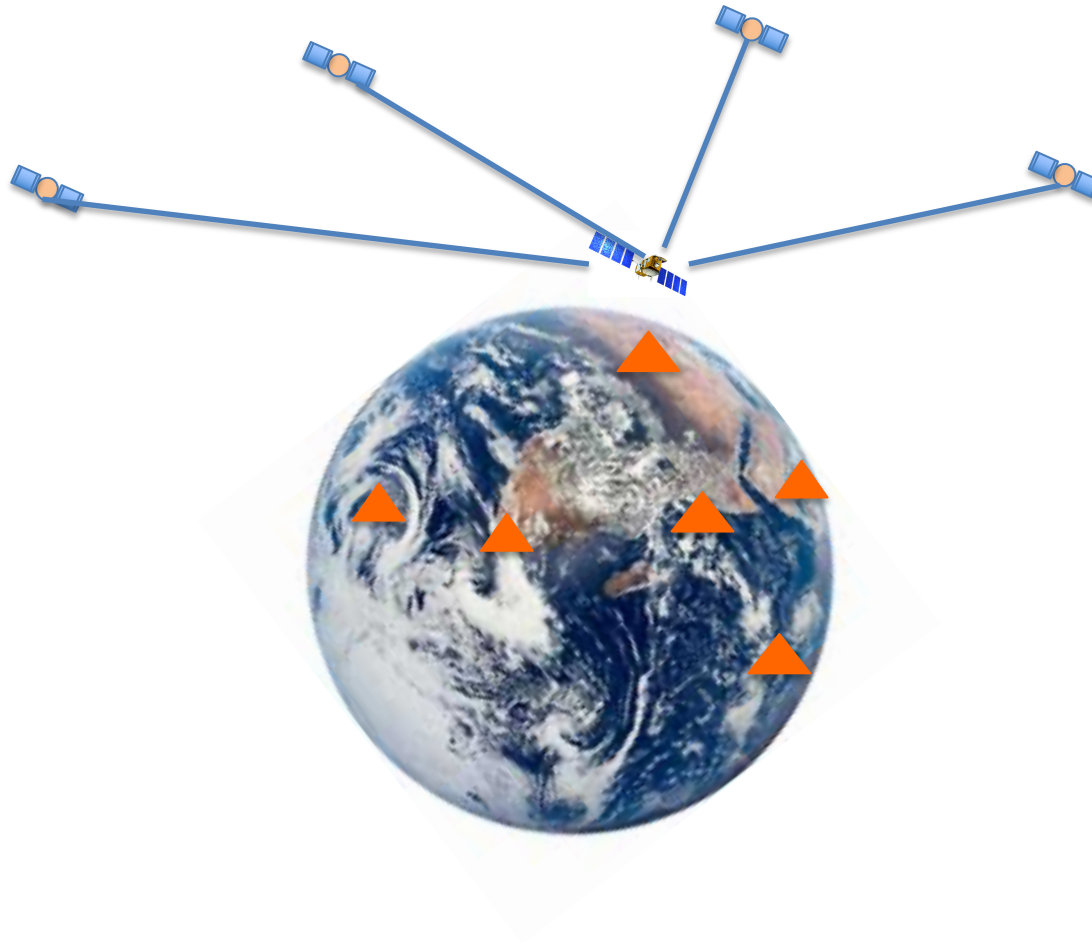
# Reference Frame via GPS

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# Reference Frame via GPS

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# Coordinate Systems for GPS Orbit Determination

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- Measurement tied to a ground stations, defined in a reference frame;
- Gravity model defined in Earth-Fixed system centered at Earth's Center of Mass (CM);
- Orbit integration performed in inertial coordinate system.
- Transformation between the Earth-Centered Inertial (ECI) system and the Earth-Centered Earth-fixed (ECEF) system is

$$r_i = PNUXY r_e$$

*P* – Precession; *N* – Nutation; *U* – Earth rotation; *X*, *Y* – Polar motion.

# JPL “Fiducial” GPS Product

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- Expressed in IGb08 reference frame, in which linear motion of geocenter is included in station coordinates definition but annual motion is not accounted for;
- LEO POD results using this product is also expressed in IGb08;
- Transformation between the Earth-Centered Inertial system and the Reference frame is

$$r_i = PNUXY (r_f - \Delta r_g)$$

$\Delta r_g$  – location of geocenter in the reference frame. This definition is consistent with the geocenter motion CM-CN.

# In the Measurement Equation

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GPS Measurements can be expressed as

$$\rho = |R - r|$$

$R$  -- receiver position vector;  $r$  -- transmitter position vector.

Both are in ECI system, transformed from the reference frame whenever necessary:

ground receiver –  $R$  is transformed from reference frame;

fixed GPS orbit –  $r$  is transformed from reference frame (of the GPS product).

# Strategy for GRACE satellites POD

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**Orbit arc length: 24-hour.**

**Gravity model: background GIF-48 180x180, estimate 20x20.**

**Accelerometer data: estimate bias, bias rate and scale for each component.**

**GPS data: 30-second PC and LC, estimate white noise clock bias and phase bias.**

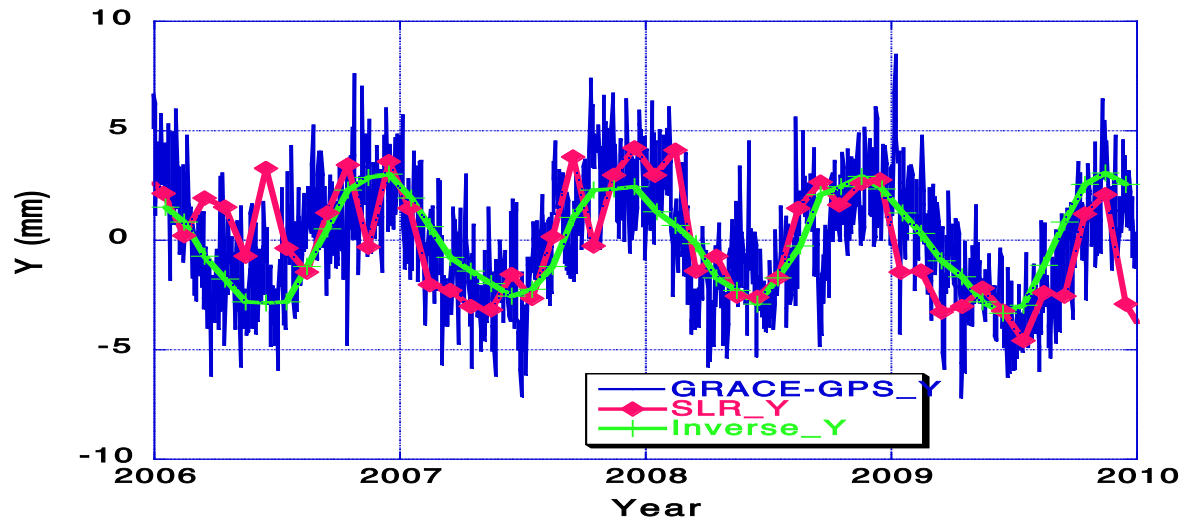
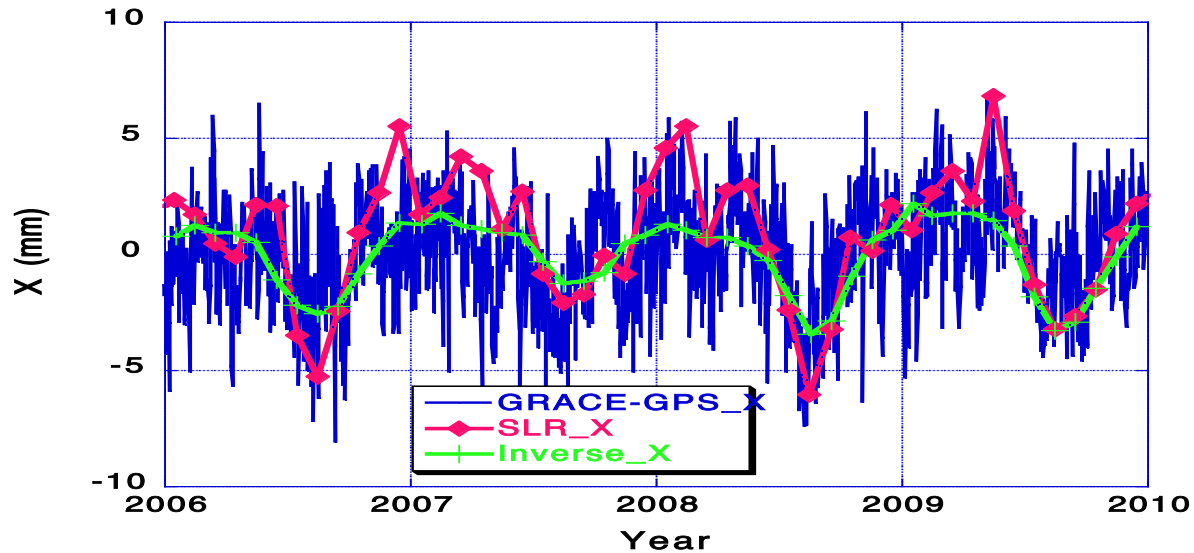
**Stochastic acc: estimate residual acceleration components along SRF axes.**

**CM location: estimate constant X, Y, and Z components in EF system, and X, Y in ECI system.**

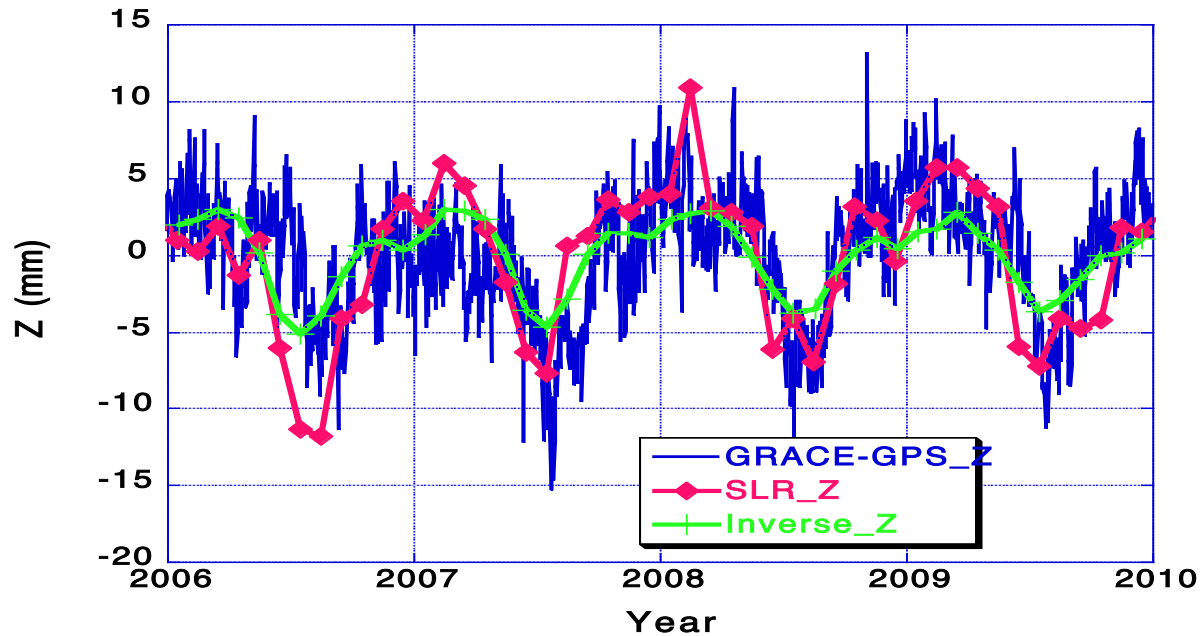


# Combined solution from both GRACE satellites

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# Combined solution from both GRACE satellites



| Solution  | X      |        | Y      |         | Z      |        |
|-----------|--------|--------|--------|---------|--------|--------|
|           | Amp    | Phase  | Amp    | Phase   | Amp    | Phase  |
| GRACE GPS | 1.1 mm | 49 day | 2.7 mm | 332 day | 3.5 mm | 35 day |
| CSR/SLR   | 2.6 mm | 58 day | 2.3 mm | 317 day | 4.7 mm | 28 day |
| Inverse   | 1.9 mm | 53 day | 2.8 mm | 333 day | 2.9 mm | 31 day |

# Strategy for LEOs without accelerometer

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**Orbit arc length: 24-hour.**

**Gravity model: background GIF-48 180x180, estimate 20x20.**

**Surface force model: estimate Cd, solar pressure scale, and once-per-revolution empirical forces**

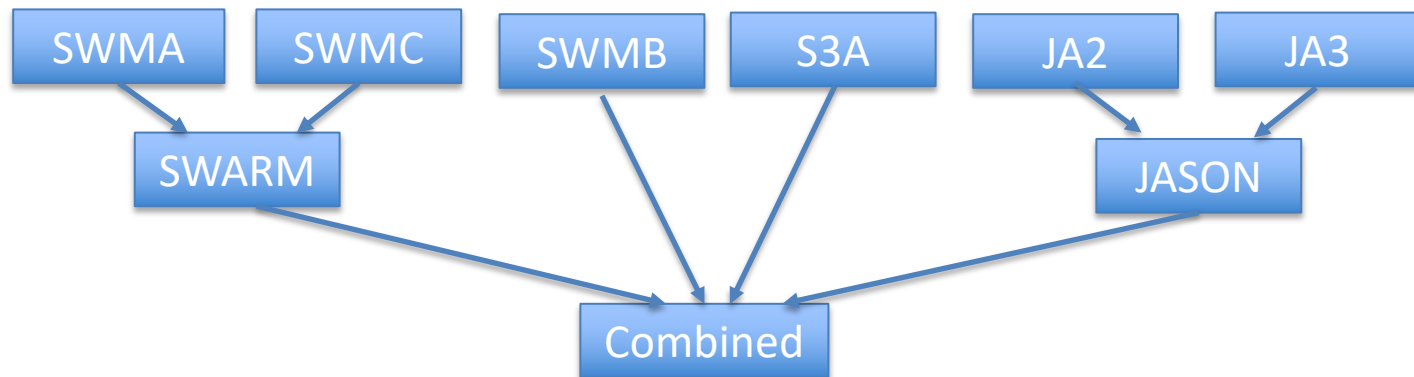
**GPS data: 30-second PC and LC, estimate white noise clock bias and phase bias.**

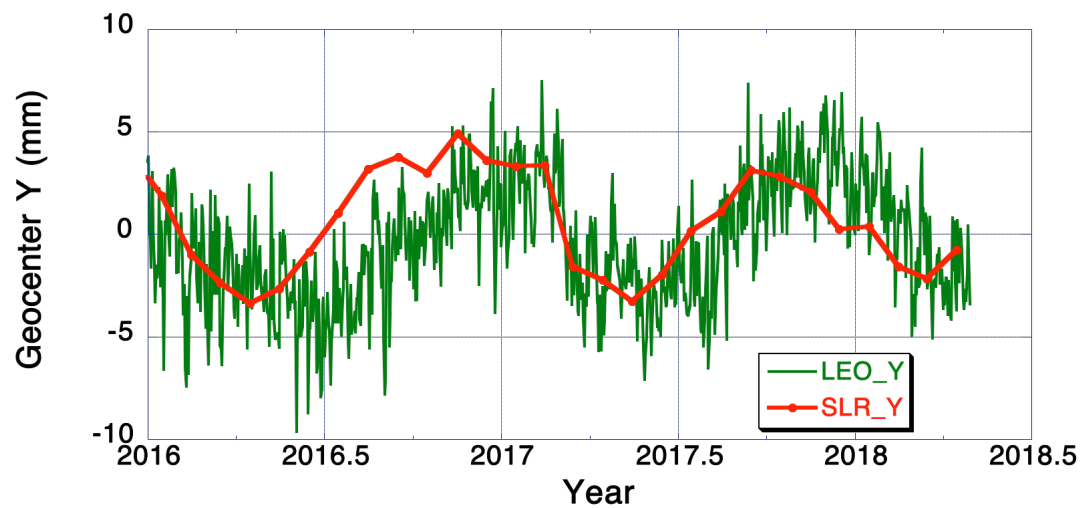
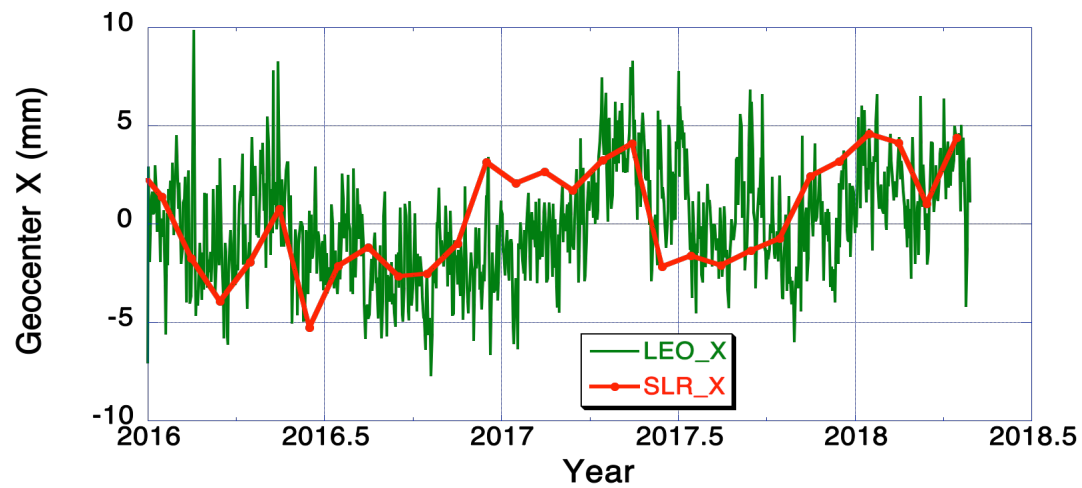
**Stochastic acc: estimate residual acceleration components along orbital frame.**

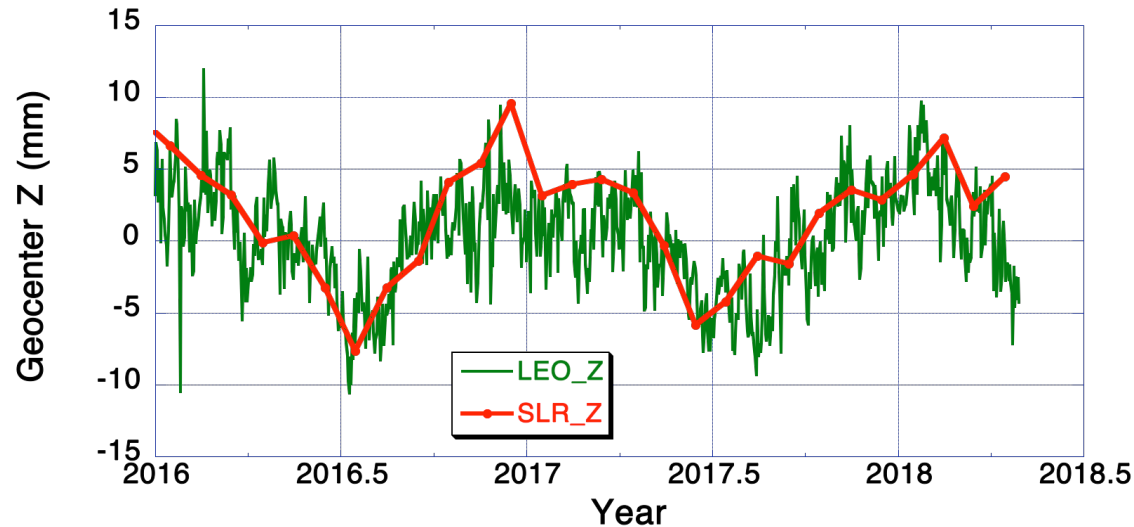
**CM location: estimate constant X, Y, and Z components in EF system, and X, Y in ECI system.**

## Combining solutions from individual orbits:

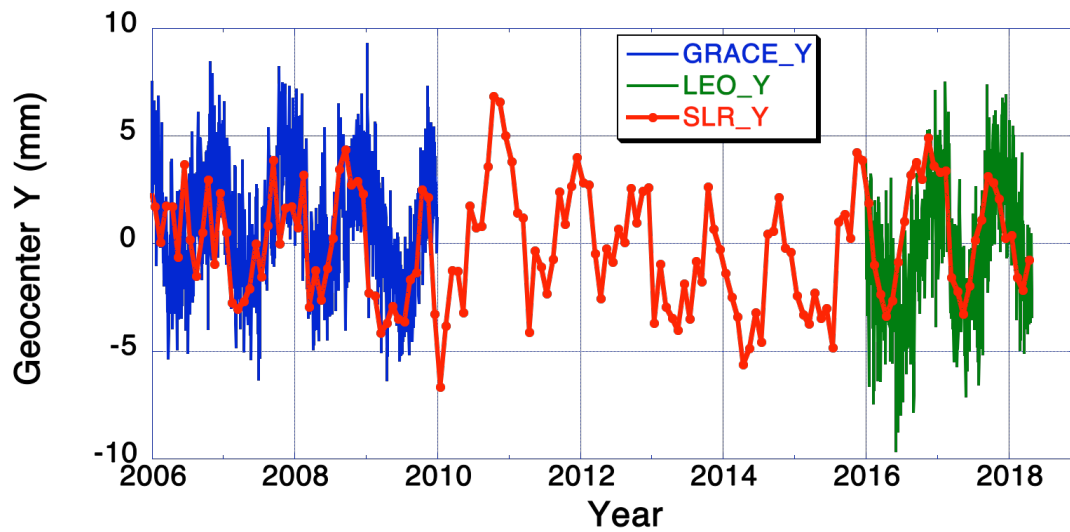
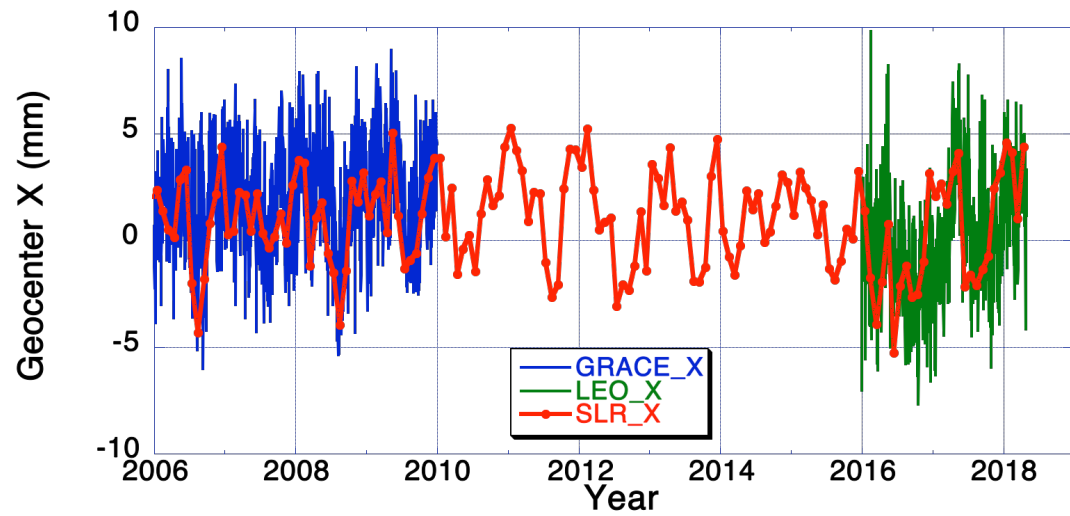
Solutions from 6 satellites in 4 different orbit planes are combined. Satellites in same orbital plane suffer the similar systematic errors, solutions from those satellites are combined first and treated as one solution with equivalent weight to others.

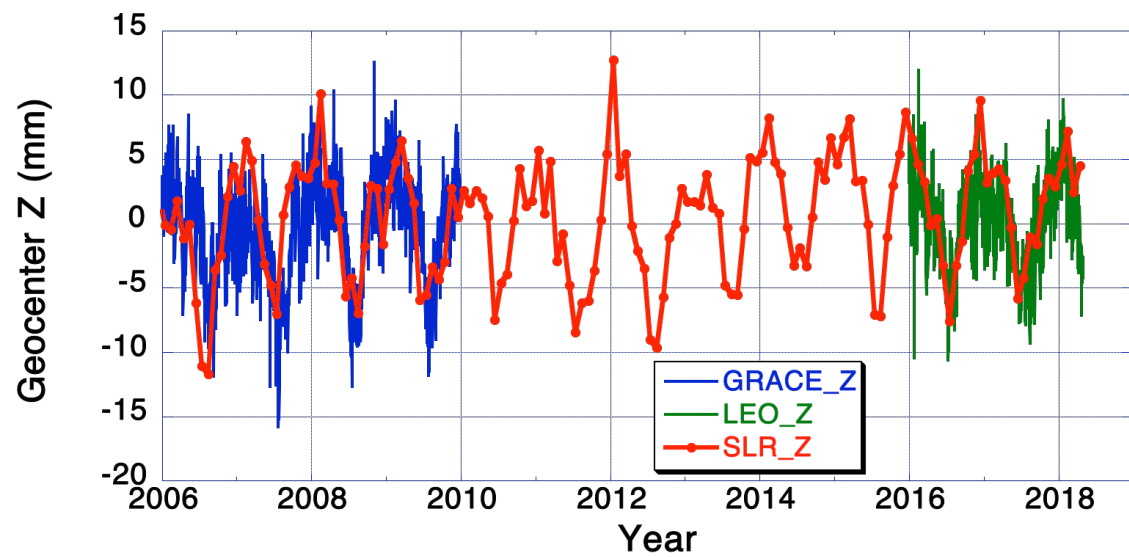






**The combined estimates agree with those estimated from SLR tracking data. They are also consistent with those estimated from GRACE-GPS and accelerometer data, as both agree with the SLR solution over time.**







# Summary

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- **Earth's center of mass location in a reference frame can be determined using LEO GPS tracking data through orbit determination with GPS orbits and clocks fixed in that reference frame.**
- **Averaged from multiple satellites, solutions with or without accelerometer data are consistent, as compared to the results from SLR tracking data.**